

Chapter 11

Work and Energy

Multiple Choice Questions

1. When a body falls freely towards the earth, then its total energy

- (a) increases**
- (b) decreases**
- (c) remains constant**
- (d) first increases and then decreases**

Soln:

Answer is (c) remains constant

Explanation

Body falling freely towards the earth possess same kinetic and potential energy and it follows Law of conservation of energy hence its total energy remains constant.

2. A car is accelerated on a levelled road and attains a velocity 4 times of its initial velocity. In this process the potential energy of the car

- (a) does not change**
- (b) becomes twice to that of initial**
- (c) becomes 4 times that of initial**
- (d) becomes 16 times that of initial**

Soln:

Answer is (a) does not change

Explanation:

Potential energy is the product of height, mass and gravity. Hence height is a factor in determining potential energy. Here the height does not change hence potential energy of the car does not change.

3. In case of negative work the angle between the force and displacement is

- (a) 0°**
- (b) 45°**
- (c) 90°**
- (d) 180°**

Soln:

Answer is (d) 180°

Explanation:

workdone = $FS \cos\theta$

$\cos 180^\circ = -1$

Hence the answer is 180°

4. An iron sphere of mass 10 kg has the same diameter as an aluminium sphere of mass is 3.5 kg. Both spheres are dropped simultaneously from a tower. When they are 10 m above the ground, they have the same

- (a) acceleration**
- (b) momenta**
- (c) potential energy**
- (d) kinetic energy**

Soln:

Momentum, potential energy and kinetic energy varies with weight. But in this case acceleration is because of acceleration due to gravity which is independent of mass hence acceleration is the right answer.

5. A girl is carrying a school bag of 3 kg mass on her back and moves 200 m on a levelled road. The work done against the gravitational force will be ($g = 10 \text{ m s}^{-2}$)

- (a) $6 \times 10^3 \text{ J}$**
- (b) 6 J**
- (c) 0.6 J**
- (d) zero**

Soln:

Here Direction of workdone is perpendicular to gravitational force direction. Hence the workdone against the gravity is zero.

6. Which one of the following is not the unit of energy?

- (a) joule**
- (b) newton metre**
- (c) kilowatt**
- (d) kilowatt hour**

Soln:

Answer is (c) kilowatt

Explanation:

Kilowatt is SI Unit of electrical power

7. The work done on an object does not depend upon the

- (a) displacement**
- (b) force applied**
- (c) angle between force and displacement**
- (d) initial velocity of the object**

Soln:

Answer is (d) initial velocity of the object

Explanation:

Workdone is the product of force and displacement hence force and displacement are the required attributes for the work to be done. But workdone is not dependent of initial velocity.

8. Water stored in a dam possesses

- (a) no energy**
- (b) electrical energy**
- (c) kinetic energy**
- (d) potential energy**

Soln:

Answer is (d) potential energy

Explanation:

Potential energy is the energy stored in an object because of the position. Water in the dam possess energy because of position hence it is potential energy.

9. A body is falling from a height h . After it has fallen a height $\frac{h}{2}$, it will possess

- (a) only potential energy**
- (b) only kinetic energy**
- (c) half potential and half kinetic energy**
- (d) more kinetic and less potential energy**

Soln:

Answer is (c) half potential and half kinetic energy

Explanation:

When body is at height h , its potential will be hundred percent and kinetic energy will be zero. In the same way when body reached ground its potential energy will be zero and kinetic energy will be maximum. At height $\frac{h}{2}$ both potential energy and kinetic energy of the body will be half.

Short answer Questions

10. A rocket is moving up with a velocity v . If the velocity of this rocket is suddenly tripled, what will be the ratio of two kinetic energies?

Soln:

Initial velocity= $v=3v$

Initial kinetic energy= $\frac{1}{2}v^2$

Kinetic energy= $\frac{1}{2}v^2$

$$\frac{1}{2}m(3v)^2 = 9\left(\frac{1}{2}mv^2\right)$$

Ratio between Initial kinetic energy and final kinetic energy is 1:9

11. Avinash can run with a speed of 8 m s^{-1} against the frictional force of 10 N , and Kapil can move with a speed of 3 m s^{-1} against the frictional force of 25 N . Who is more powerful and why?

Soln:

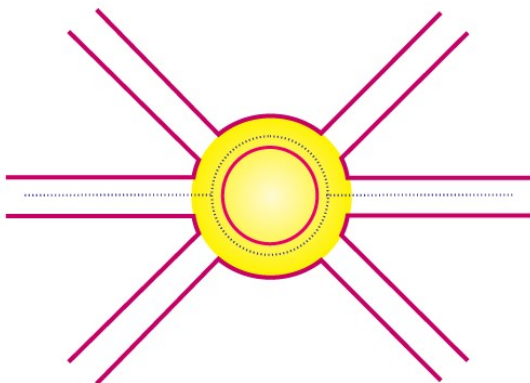
$$P = f \times v$$

$$P_1 = 10 \times 8 = 80 \text{ W}$$

$$P_2 = 25 \times 3 = 75 \text{ W}$$

Hence Avinash is more powerful than Kapil

12. A boy is moving on a straight road against a frictional force of 5 N . After travelling a distance of 1.5 km he forgot the correct path at a round about (Fig. 11.1) of radius 100 m . However, he moves on the circular path for one and half cycle and then he moves forward upto 2.0 km . Calculate the work done by him.



Soln:

Total distance travelled by the boy = $1500 \text{ m} + 200 \text{ m} + (1.5 \times 2 \pi r)$

Total distance travelled by the boy = $1500 \text{ m} + 200 \text{ m} + (1.5 \times 2 \times 3.14 \times 100) = 4442 \text{ m}$

Frictional force = 5 N

Workdone = force \times Displacement

Workdone = $5 \times 4442 = 22210 \text{ J}$

13. Can any object have mechanical energy even if its momentum is zero? Explain.

Soln:

Momentum is the product of mass and velocity. If the body is at rest its velocity will be zero. If it is at rest at height it possesses gravitational potential energy hence mechanical energy.

14. Can any object have momentum even if its mechanical energy is zero? Explain.

Soln:

No, Because its potential and kinetic energy are zero.

15. The power of a motor pump is 2 kW. How much water per minute the pump can raise to a height of 10 m? (Given $g = 10 \text{ m s}^{-2}$)

Soln:

Power of pump = $2 \text{ kW} = 2000 \text{ W}$

Time (t) = 60 sec

Height (h) = 10 m $g = 10 \text{ m/s}^2$

Power = work done per unit time.

Work done = $mgh = m \times 10 \times 10 = 100m$

$$2000 \text{ W} = \frac{10m}{60}$$

Therefore, $m = 1200 \text{ kg}$ So, the pump can raise 1200 kg of water in one minute.

16. The weight of a person on a planet A is about half that on the earth. He can jump upto 0.4 m height on the surface of the earth. How high he can jump on the planet A?

Soln:

Person on Planet A can jump a height of 0.8 m because weight of person on planet A is half the weight that of earth. Hence acceleration due to gravity on planet A will also be half of that on earth.

17. The velocity of a body moving in a straight line is increased by applying a constant force F, for some distance in the direction of the motion. Prove that the increase in the kinetic energy of the body is equal to the work done by the force on the body.

Soln:

$$v^2 - u^2 = 2as$$

$$s = \frac{v^2 - u^2}{2a}$$

$$F = ma$$

$$W = ma \left(\frac{v^2 - u^2}{2a} \right)$$

$$= \frac{1}{2}mv^2 - \frac{1}{2}mu^2$$

$$= (K.E)_f - (K.E)_i$$

18. Is it possible that an object is in the state of accelerated motion due to external force acting on it, but no work is being done by the force. Explain it with an example.

Soln:

Force always acts in perpendicular to the displacement direction. If the object is moving in circular path then no work will be done despite of action of force.

19. A ball is dropped from a height of 10 m. If the energy of the ball reduces by 40% after striking the ground, how much high can the ball bounce back? ($g = 10 \text{ m s}^{-2}$).

Soln:

$$mgh = m \times 10 \times 10 = 100m \text{ joules}$$

when 40% energy is reduced remaining energy will be 60mjoules

$$\text{Hence } 60 = m \times 10 \times h$$

$$H = 6m$$

20. If an electric iron of 1200 W is used for 30 minutes everyday, find electric energy consumed in the month of April.

Soln:

$$\text{Power of electric iron} = 1200W$$

$$\begin{aligned} \text{Usage per day} &= 30 \text{ min} \\ &= 30/60 \text{ hrs} \\ &= 0.5 \text{ hrs} \end{aligned}$$

Number of days in the month of April=30days

$$\begin{aligned}\text{Electrical energy consumed, } E &= P \times t \quad 1200 \times 0.5 \times 30 \\ &= 18000 \text{ WH} \\ &= 18 \text{ KWH} \\ &= 18 \text{ units}\end{aligned}$$

Therefore, The Total Electricity consumed in april month is 18 units

Long answer Questions

21. A light and a heavy object have the same momentum. Find out the ratio of their kinetic energies. Which one has a larger kinetic energy?

Soln:

$$\begin{aligned}\text{Kinetic energy equation: } E_k &= \frac{1}{2}mv^2 \\ E_k &= \frac{1}{2}mv^2\end{aligned}$$

$$\text{Momentum equation: } p = mv$$

$$p = mv$$

$$\text{Kinetic energy equation in terms of momentum: } E_k = \frac{p^2}{2m}$$

Kinetic energy of two objects will be same if their mass and momentum are same. Among light and heavy bodies Heavy body has highest momentum. When the momentum is equal light body has more kinetic energy.

22. An automobile engine propels a 1000 kg car (A) along a levelled road at a speed of 36 km h⁻¹. Find the power if the opposing frictional force is 100 N. Now, suppose after travelling a distance of 200 m, this car collides with another stationary car (B) of same mass and comes to rest. Let its engine also stop at the same time. Now car (B) starts moving on the same level road without getting its engine started. Find the speed of the car (B) just after the collision.

Soln:

$$m(A) = m(B) = 1000 \text{ kg.}$$

$$v = 36 \text{ km/h} = 10 \text{ m/s}$$

$$\text{Frictional force} = 100 \text{ N}$$

car A moves with a uniform speed, which means engine of car applies a force equal to the frictional force

$$\text{Power} = \text{Force} \times \text{distance} / \text{time} = F \cdot V$$

$$= 100 \text{ N} \times 10 \text{ m/s} = 1000 \text{ W}$$

After collision $m_A u_A + m_B u_B = m_A v_A + m_B v_B$.

$$\begin{aligned} & 1000 \times 10 + 1000 \times 0 \\ & = 1000 \times 0 + 1000 \times v_B \quad v_B \\ & = 10 \text{ m s}^{-1} \end{aligned}$$

23. A girl having mass of 35 kg sits on a trolley of mass 5 kg. The trolley is given an initial velocity of 4 m s⁻¹ by applying a force. The trolley comes to rest after traversing a distance of 16 m. (a) How much work is done on the trolley? (b) How much work is done by the girl?

Soln:

(a)

Initial velocity of the trolley, $u = 4 \text{ m/s}$

Final velocity of the trolley $v = 0$

Mass of the trolley $m = 5 \text{ kg}$

Distance covered by the trolley before coming to rest, $s = 16 \text{ m}$

From Equation 2 as $v^2 = u^2 + 2as$,

$$\begin{aligned} a & = \frac{v^2 - u^2}{2s} \\ & = \frac{0 - (4)^2}{2 \times 16} \\ & = -0.5 \text{ m/s}^2 \end{aligned}$$

Force (frictional) acting on the trolley $= ma$

$$= 40 (-0.5)$$

$$= -20 \text{ N}$$

Work done on the trolley $= Fs = (20 \text{ N}) (16 \text{ m})$

$$= 320 \text{ J}$$

(b) Since the girl does not move w.r.t. the trolley (as she is sitting on it), work done by the girl $= 0$.

24. Four men lift a 250 kg box to a height of 1 m and hold it without raising or lowering it.

(a) How much work is done by the men in lifting the box?

(b) How much work do they do in just holding it?

(c) Why do they get tired while holding it? ($g = 10 \text{ m s}^{-2}$)

Soln:

(a)

$$F = 250 \text{ kg} \times g = 2500 \text{ N}$$

$$S = 1 \text{ m}$$

$$W = F \cdot s = 2500 \text{ Nm} = 2500 \text{ J}$$

(b)

While holding box there is no displacement hence workdone is zero

c) While holding the box they apply muscular force which is equal and opposite to the gravitational force hence they feel tired while holding box.

25. What is power? How do you differentiate kilowatt from kilowatt hour? The Jog Falls in Karnataka state are nearly 20 m high. 2000 tonnes of water falls from it in a minute. Calculate the equivalent power if all this energy can be utilized? ($g = 10 \text{ m s}^{-2}$)

Soln:

Power is the rate of transfer of energy or rate of doing work. Watt is the unit of power and kilowatt is 1000 watts.

$$h = 20 \text{ m, and mass} = 2000 \times 10^3 \text{ kg} \\ = 2 \times 10^6 \text{ kg}$$

$$\text{Power} = m g h / t \\ = \frac{2 \times 10^6 \times 10 \times 20}{60}$$

$$w = \frac{4}{3} \times 10^7 \text{ w} =$$

$$\frac{4}{3} \times 10^7 \text{ w}$$

26. How is the power related to the speed at which a body can be lifted? How many kilograms will a man working at the power of 100 W, be able to lift at constant speed of 1 m s^{-1} vertically? ($g = 10 \text{ m s}^{-2}$)

Soln:

$$\begin{aligned} \text{Power} &= \text{work/time} \\ \text{work} &= \text{force} \times \text{displacement} \\ \text{force} &= \text{mass} \times \text{acceleration} \\ \text{acceleration} &= \text{velocity/time} \end{aligned}$$

Therefore

$$\text{Power} = \frac{\text{velocity} \times \text{mass} \times \text{displacement}}{\text{time} \times \text{time}}$$

Here

$$\text{Power, } P = 100 \text{ W}$$

$$\text{velocity, } v = 1 \text{ m/s}$$

$$\text{since time, } t = 1 \text{ s}$$

$$\text{displacement, } s = 1 \text{ m}$$

$$\text{acceleration, } a = 10 \text{ m/s}^2$$

$$\text{From equation } P = \frac{m \times a \times s}{t}$$

$$100 = m \times 10$$

$$m = 10$$

27. Define watt. Express kilowatt in terms of joule per second. A 150 kg car engine develops 500 W for each kg. What force does it exert in moving the car at a speed of 20 m s⁻¹?

Soln:

Power of an object which does work at 1 Joules/sec is called watt

$$1 \text{ watt} = \frac{\text{Joule}}{\text{second}}$$

$$1 \text{ kilowatt} = 1000 \text{ watts} = 1000 \text{ J/sec}$$

$$\text{mass of car} = 150 \text{ kg}$$

$$\text{power for each kg} = 500 \times 150 = 7500 \text{ w}$$

$$\text{speed} = 20 \text{ m/s}$$

$$\text{power} = \text{Force} \times v$$

$$\therefore \text{force} = \text{power} / v$$

$$\frac{7500}{20}$$

$$= 3750 \text{ N}$$

28. Compare the power at which each of the following is moving upwards against the force of gravity? (given $g = 10 \text{ m s}^{-2}$) (i) a butterfly of mass 1.0 g that flies upward at a rate of 0.5 m s⁻¹. (ii) a 250 g squirrel climbing up on a tree at a rate of 0.5 m s⁻¹.

Soln:

i) Butterfly force = $mg = 1/100$
power = $f \times s \div t$. { $s \div t = \text{velocity}$ }
power = $1 \div 100 \times .5$
power = $1 \div 200 \text{ W}$

ii) squirrel force = $mg = 25$
power = $25 \times .5$
power = 12.5 W