

MATHEMATICS
WORKSHEET_210925
CHAPTER 07 TRIANGLES

SUBJECT: MATHEMATICS
CLASS : IX

MAX. MARKS : 40
DURATION : $1\frac{1}{2}$ hrs

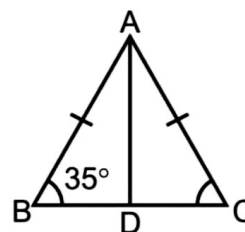
General Instructions:

- (i). All questions are compulsory.
- (ii). This question paper contains 20 questions divided into five Sections A, B, C, D and E.
- (iii). **Section A** comprises of 10 MCQs of 1 mark each. **Section B** comprises of 4 questions of 2 marks each. **Section C** comprises of 3 questions of 3 marks each. **Section D** comprises of 1 question of 5 marks each and **Section E** comprises of 2 Case Study Based Questions of 4 marks each.
- (iv). There is no overall choice.
- (v). **Use of Calculators is not permitted**

SECTION – A

Questions 1 to 10 carry 1 mark each.

1. Given two right-angled triangles ABC and PRQ, such that $\angle A = 30^\circ$, $\angle Q = 30^\circ$ and $AC = QP$. Write the correspondence if triangles are congruent.
- (a) $\triangle ABC \cong \triangle PQR$ (b) $\triangle ABC \cong \triangle PRQ$
(c) $\triangle ABC \cong \triangle RQP$ (d) $\triangle ABC \cong \triangle QRP$



2. In the given figure, AD is the median, then $\angle BAD$ is
- (a) 35° (b) 70° (c) 110° (d) 55°
3. It is given that $\triangle ABC \cong \triangle FDE$ and $AB = 5$ cm, $\angle B = 40^\circ$ and $\angle A = 80^\circ$. Then which of the following is true?
- (a) $DF = 5$ cm, $\angle F = 60^\circ$ (b) $DF = 5$ cm, $\angle E = 60^\circ$
(c) $DE = 5$ cm, $\angle E = 60^\circ$ (d) $DE = 5$ cm, $\angle D = 40^\circ$
4. If $\triangle ACB \cong \triangle EDF$, then which of the following equations is/are true?
- (I) $AC = ED$
(II) $\angle C = \angle F$
(III) $AB = EF$
- (a) Only (I) (b) (I) and (III) (c) (II) and (III) (d) All of these
5. If $AB = QR$, $BC = PR$ and $CA = PQ$ in $\triangle ABC$ and $\triangle PQR$, then:
- (a) $\triangle ABC \cong \triangle PQR$ (b) $\triangle CBA \cong \triangle PRQ$ (c) $\triangle BAC \cong \triangle RPQ$ (d) $\triangle BCA \cong \triangle PQR$
6. If in $\triangle ACB$ and $\triangle PQR$, $AC = PQ$ and $BC = RQ$, then to show $\triangle ACB \cong \triangle PQR$ by SAS congruence rule which one of the following is needed?
- (a) $\angle A = \angle P$ (b) $\angle A = \angle Q$ (c) $\angle B = \angle R$ (d) $\angle C = \angle Q$
7. In $\triangle ABC$, $BC = AB$ and $\angle B = 80^\circ$, then $\angle A$ is equal to:
- (a) 80° (b) 40° (c) 50° (d) 100°
8. If $\triangle ABC \cong \triangle PQR$ and $\triangle ABC$ is not congruent to $\triangle RPQ$, then which of the following is not true?
- (a) $BC = PQ$ (b) $AC = PR$ (c) $QR = BC$ (d) $AB = PQ$

In the following questions 9 and 10, a statement of assertion (A) is followed by a statement of Reason (R). Choose the correct answer out of the following choices.

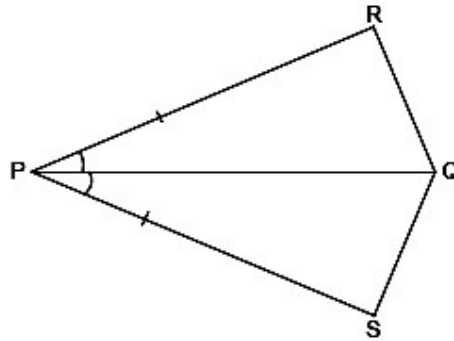
- (a) Both A and R are true and R is the correct explanation of A.

- (b) Both A and R are true but R is not the correct explanation of A.
 (c) A is true but R is false.
 (d) A is false but R is true.

9. **Assertion (A):** If we draw two triangles with angles 30° , 70° , and 80° and the length of the sides of one triangle be different than that of the corresponding sides of the other triangle then two triangles are not congruent.

Reason (R): If two triangles are constructed which have all corresponding angles equal but have unequal corresponding sides, then two triangles cannot be congruent to each other.

10. **Assertion (A):** In a quadrilateral PQRS, $PR = PS$ and PQ bisect $\angle P$ by SAS congruency criteria.

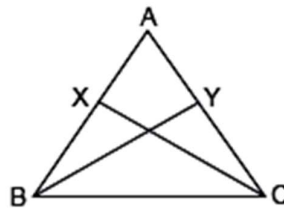


Reason (R): SAS congruency axiom state that if two sides and their including angle of one triangle is equal to the corresponding two sides and including angle of other triangle, then Both the triangles are congruent.

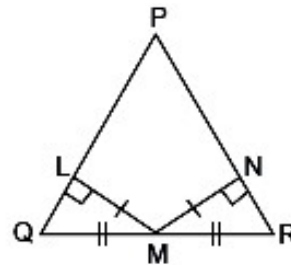
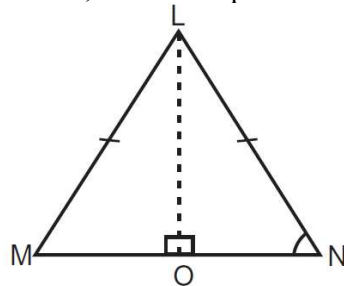
SECTION – B

Questions 11 to 14 carry 2 marks each.

11. In the figure below, ABC is a triangle in which $AB = AC$. X and Y are points on AB and AC such that $AX = AY$. Prove that $\triangle ABY \cong \triangle ACX$.

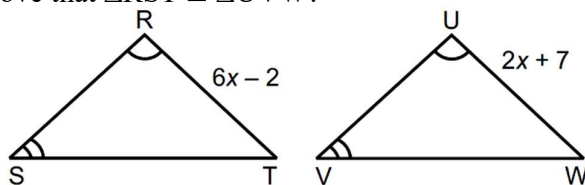


12. In the below left figure, $\triangle LMN$ is an isosceles triangle, where $LM = LN$ and LO, is an angle bisector of $\angle MLN$, Prove that point 'O' is the mid-point of side MN.



13. In the above right sided figure, $LM = MN$, $QM = MR$, $ML \perp PQ$ and $MN \perp PR$. Prove that $PQ = PR$.

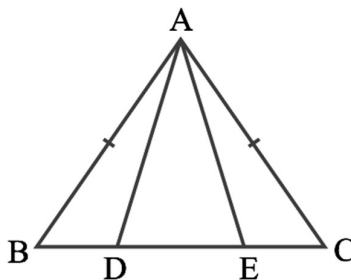
14. In $\triangle RST$, $RT = 6x - 2$. In $\triangle UVW$, $UW = 2x + 7$, $\angle R = \angle U$, and $\angle S = \angle V$. What must be the value of x in order to prove that $\triangle RST \cong \triangle UVW$?



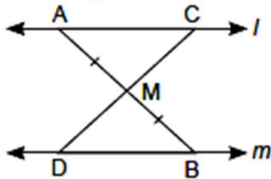
SECTION – C

Questions 15 to 17 carry 3 marks each.

15. In the given figure, $AB = AC$ and $BE = CD$. Prove that $AD = AE$.



16. In the given figure, $l \parallel m$ and M is the mid-point of line segment AB . Prove that M is also the mid-point of any line segment CD having its end points C and D on l and m respectively.



17. Prove that angles opposite to equal sides of an isosceles triangle are equal.

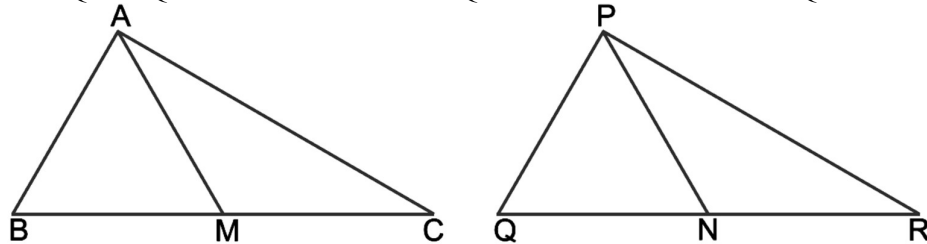
OR

$\triangle ABC$ is an isosceles triangle in which $AB = AC$. Side BA is produced to D such that $AD = AB$. Show that $\angle BCD$ is a right angle.

SECTION – D

Questions 18 carry 5 marks.

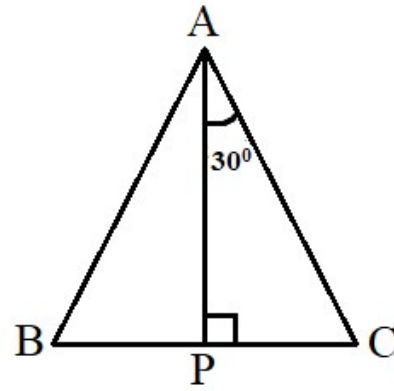
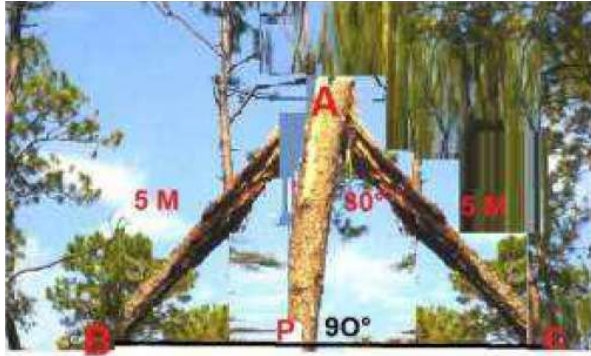
18. In the below figure, two sides AB and BC and median AM of one triangle ABC are respectively equal to sides PQ and QR and median PN of $\triangle PQR$. Show that $\triangle ABC \cong \triangle PQR$.



SECTION – E (Case Study Based Questions)

Questions 19 to 20 carry 4 marks each.

19. Aditya and his friends went to a forest, they saw a big tree got broken due to heavy rain and wind. Due to this rain the big branches AB and AC with lengths 5m fell down on the ground. Branch AC makes an angle of 30° with the main tree AP . The distance of Point B from P is 4 m. You can observe that $\triangle ABP$ is congruent to $\triangle ACP$.

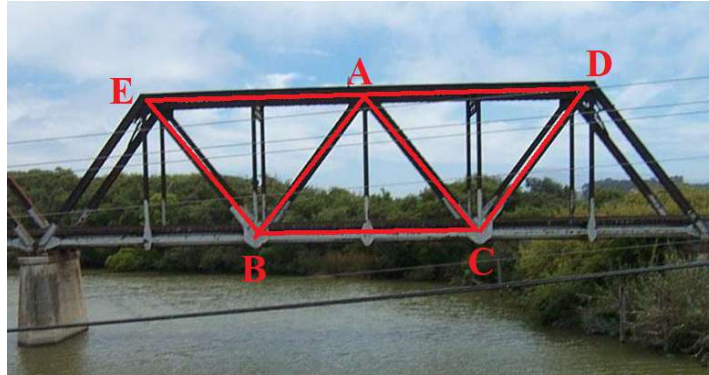


- (a) Show that $\triangle ABP$ is congruent to $\triangle ACP$ (1)
 (b) Find the value of $\angle ACP$? (2)

OR

- What is the total height of the tree? (2)
 (c) Find the value of $\angle BAP$? (1)

20. Truss bridges are formed with a structure of connected elements that form triangular structures to make up the bridge. Trusses are the triangles that connect to the top and bottom cord and two end posts. You can see that there are some triangular shapes are shown in the picture given alongside and these are represented as $\triangle ABC$, $\triangle CAD$, and $\triangle BEA$.



- (a) If $AB = CD$ and $AD = CB$, then prove $\triangle ABC \cong \triangle CDA$
 (b) If $AB = 7.5$ m, $AC = 4.5$ m and $BC = 5$ m. Find the perimeter of $\triangle ACD$, if $\triangle ABC \cong \triangle CDA$ by SSS congruence rule.
 (c) If $\triangle ABC \cong \triangle FDE$, $AB = 5$ cm, $\angle B = 40^\circ$ and $\angle A = 80^\circ$. Then find the length of DF and $\angle E$.

